Investigation of the Effect of External Local Sealing Loads on the Well Support

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ARTICLE INFO

Article Type: Research Article
Keywords:
Casing
Cement
Pressure
Cryolithozone
External local sealing loads
Timeline:
Received: August 11, 2021
Accepted: September 20, 2021
Published: October 18, 2021
DOI: https://doi.org/10.15377/2409-787X.2021.08.7

ABSTRACT

The article presents the definition of problems in the well support from external local sealing loads. The conditions of local sealing loads are identified. The calculations were carried out according to the equations. A model of the stress-strain state in the well support has been created. The parameters of the effect of compression on the absolute value of strength are determined.
1. Introduction

The main cause of deformation is the formation of fluid in the annulus between the casing and tubing. After freezing, this liquid changes from liquid to solid. The pressure then destroys the casing lining and cement sheath. In general, this opinion is correct. However, the studies do not include the propagation of lateral and normal stresses in cement, as well as the effect of the presence (or absence) of adhesion and the effect of these elements on the strength of the entire structure. The above facts and the occurrence of problems in operation became the reason for the study [1].

The main reasons for the formation of the external sealing pressure are the freezing pressure in permafrost and its pressure in the zone of rock flow. As a rule, this pressure is local; therefore, it obeys the mechanics of a continuous medium [2].

2. Materials and Methods

The limiting state of the casing string can be characterized by the occurrence of plastic deformation in the inner casing, which is preceded by collapse. Moreover, it retains the load-bearing capacity. The casing and cement sheathing of other pipes bonded together will be in an elastoplastic or plastic region. During volumetric compression of the cement sheath, it is transformed into an elastoplastic material [3].

Thus, the strength of the casing support is increased by converting the entire system from brittle to ductile. The entire process of material destruction begins with microcracks. The plastic layer of one of the materials does not turn into the second layer until it reaches the stress limit. When the layer in the casing lining passes into the plastic stage, the total pressure completely passes through this layer to the next layer.

Currently, there are many varieties of the elastic and plastic range of casing pipes and cement sheath, and in general, depends on the pressure value, design features of the casing string, and the physical and mechanical characteristics of its layers. Initially, in the zone of elastoplastic deformations, the outer casing is distributed along the pipe and then along the rest of the casing [4].

The value of pressure in the elastoplastic region and the plastic region of the well casing and cement sheath is based on solving a system of equations.

\[
\begin{align*}
\sigma_{rej} &= -\sigma_{rjj} + \frac{2 \cdot \sigma_{sj}}{\sqrt{3}} \cdot \ln \frac{r}{r_j}; \\
\sigma_{\theta ej} &= -\sigma_{rjj} + \frac{2 \cdot \sigma_{sj}}{\sqrt{3}} \cdot \left(1 + \ln \frac{r}{r_j}\right);
\end{align*}
\]

It is equivalent for all layers of the well casing at the interface of the formation boundaries and during the transition from elastic to plastic \((r_j \leq r \leq \rho_j)\)

where \(\rho_j\) - radius of plasticity; \(\sigma_{rjj}\) - radial pressure in the inner regions of the outer pipe and cement; \(\sigma_{rj}^+\) - radial pressure of the material yield point in the \(j^{th}\) layer [5].

Table 1 shows the bearing capacity of the casing in the zones of elastoplastic and plastic deformations.

At these values, plastic regions of various sizes are formed in the casing of a three-column well structure [6].

Table 1 presents two options for the results; the first has a modulus of elasticity \(E_1=1*10^3\) MPa for cement between the casing pipes. The second has \(E_2=1*10^4\) MPa.

As shown in Table 1, the external pressure of the casing support in the elastoplastic deformation zone is higher than in the elastic deformation zone. However, the spread of the plasticity zone in the casing pipes of the lining leads to uneven loading or loss of stability.
Table 1: Calculated values of external pressure.

<table>
<thead>
<tr>
<th>Elastoplastic area (%) in casing support with diameter and thickness of pipe wall, mm</th>
<th>Pressure (external), MPa</th>
</tr>
</thead>
<tbody>
<tr>
<td>168×12,0</td>
<td>245×13,8</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>50</td>
</tr>
</tbody>
</table>

As a result, this leads to serious well accidents. In connection with the calculation data, the resistance to casing collapse is based on its tests in the elastic deformation zone [7].

The creation of a mathematical model of the bending of a complex well design can be represented in the form of differential equations of a single-level design [8].

\[ D \left( \frac{d^4 w}{dx^4} + 4w\beta \right) = q, \]  

(2)

where $D$ - integral characteristic of the bending stiffness value of a complex well structure; $w(x)$ - bending function, m; $q$ - local load of pressure distribution in the investigated area, MPa;

For one of the layers, this expression can be transformed into the following equation:

\[ D = \sum_{i=1}^{n} \frac{E^{(i)} h^{(i)}^3}{12 (1 - \nu^{(i)})} \cdot C^{(i)}^3 \cdot \lambda, \]  

(3)

The first of the terms is represented by the stiffness value of a simple well structure, whereas the second provides for the strength of the bond between the columns [9].

where $\lambda$ -the modular value of the ratio, which can be expressed from the following equation:

\[ \lambda = \frac{\frac{d^2 w}{dx^2} \cdot \eta}{\frac{d^2 w}{dx^2} \cdot \eta - \frac{E^{(i)} h^{(i)}^3}{(1 - \nu)}} \cdot \frac{d^4 w}{dx^4} \]  

(4)

where $C^{(i)}$ - distance between the centers of adjacent layers on the surface of the borehole wall, m; $E^{(i)}$ - modulus of elastic $i$-layer; $\nu^{(i)}$ - poisson's ratio for the material of $i$-layer; $h^{(i)}$ - thickness of the $i$-layer, m; $R$ - the radius of curvature of the shell, m; $\eta$ - coefficient of adhesion shear stiffness at the contact of a cement-filling pipe, N/mm³.

\[ \beta = \sum_{i=1}^{n} \frac{E^{(i)} h^{(i)}}{4R^2 D}. \]  

(5)

The bending of a compound cylindrical shell is performed on the lateral faces of the structure for the condition of hinged support [10].

The deflection function is presented as a system of sinus functions $W(x)$ (6):
\[ W(x) = \sum_{m=1}^{\infty} W_m \sin \frac{m\pi x}{\alpha}. \]  

(6)

Deformation in the range of the line (7):

\[ q(x) = \sum_{m=1}^{\infty} q_m \sin \frac{m\pi x}{\alpha}. \]  

(7)

Thus, it is possible to calculate radial deformations (8);

\[
\sigma_x^{(1)} = \frac{d^2 w}{dx^2} \left(C^{(1)} \alpha + h^{(1)} \right) \frac{E^{(1)}}{\left(1 - \nu^{(1)}\right)^2},
\]

\[
\sigma_x^{(2)} = \frac{d^2 W h^{(2)}}{dx^2} \frac{E^{(2)}}{2 \left(1 - \nu^{(2)}\right)^2},
\]

\[
\sigma_x^{(3)} = \frac{d^2 w}{dx^2} \left(C^{(3)} \alpha + h^{(3)} \right) \frac{E^{(3)}}{\left(1 - \nu^{(3)}\right)^2},
\]

(8)

where \( \alpha \) - length in the area of local deformation [11].

The following expression gives the tangential shear stress at the boundaries of the adjacent layer:

\[
\tau_{x(xy)}^{(1)} = \eta_{x(xy)} \left[ C^{(1)} \frac{\partial w}{\partial x} + \int_0^x \frac{\partial^2 w}{\partial x^2} (Z_x - C_x^{(1)} \alpha_x^{(1)}) dx + (A_2 - A_1) \right],
\]

\[
\tau_{y(xy)}^{(1)} = \eta_{y(xy)} \left[ C^{(1)} \frac{\partial w}{\partial y} + \int_0^y \frac{\partial^2 w}{\partial y^2} (Z_y - C_y^{(1)} \alpha_y^{(1)}) dy + (A_4 - A_3) \right].
\]

(9)

where \( A_m \) - constants depending on the boundary conditions of the layer attachment [12].

Thus, according to the solution of the equations, it is possible to determine the magnitude of the local sealing loads on the investigated section of the well of a complex design.

3. Results

The difference in constants is represented as \( A_{m+1} + A_1 = 0. \)

For \( Z^1 \in \left(-\frac{h^1}{2}; \frac{h^1}{2}\right) \) is the coordinate of the point \( v_i \) - the layer in which the stress state components are formed.

Let us look at an example.

Figure 1 shows a computational model of the stress-strain state of wells with a complex casing support structure under a local axisymmetric load.

Figure 1 shows the graphs of the propagation of normal and shear stresses in the casing and cement sheath.

This example shows that the force of external pressure increases at the point of compaction where the cement comes in contact with the casing of the well.
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Main significant coefficients:

- $h^{(1)}$, $h^{(2)}$, and $h^{(3)}$ - thickness of cement and pipe walls;
- $E^{(1)}$, $E^{(3)}$, and $E^{(2)}$ - the modulus of elasticity of the pipe material and cement stone.

The values of the lower and upper levels of the casing wall thickness are taken from the standards, and the elastic modulus of the cement is in accordance with the conditions of the problem [13].

$$h^{(1)} = h^{(3)} = 8.9 \times 10^{-3} \text{ m}; \quad h^{(2)} = 29.6 \times 10^{-3} \text{ m}; \quad R = 98.8 \times 10^{-3} \text{ m}; \quad \nu = 0.100, 10^6 \text{ N / mm}^3; \quad E^{(1)} = E^{(3)} = 2.1 \times 10^5 \text{ MPa}; \quad a = 12.0 \text{ m}; \quad C^{(1)} = C^{(2)} = 23.7 \times 10^{-3} \text{ m}; \quad q = 50 \text{ MPa}; \quad \eta = 0.100, 10^6 \text{ MPa}.$$

The maximum values of the parameters of the stress-strain state of the well support are shown in Table 2.

**Table 2: Basic calculation parameters.**

<table>
<thead>
<tr>
<th>$E_{II}$, M1a</th>
<th>$\eta$, H/mm$^3$</th>
<th>$W$, mm</th>
<th>$\tau$, M1a</th>
<th>$\sigma^{(1)}$, M1a</th>
<th>$\sigma^{(1)}$, M1a</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1 \times 10^3$</td>
<td>0,0</td>
<td>0,2345</td>
<td>0,0</td>
<td>-115,7</td>
<td>-8,5</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>0,2344</td>
<td>0,5</td>
<td>-113,8</td>
<td>-6,6</td>
</tr>
<tr>
<td></td>
<td>$10^4$</td>
<td>0,1162</td>
<td>14,1</td>
<td>-102,8</td>
<td>-1,9</td>
</tr>
<tr>
<td>$5 \times 10^3$</td>
<td>0,0</td>
<td>0,2187</td>
<td>0,0</td>
<td>-107,1</td>
<td>-39,0</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>0,2187</td>
<td>0,4</td>
<td>-105,3</td>
<td>-30,8</td>
</tr>
<tr>
<td></td>
<td>$10^5$</td>
<td>0,109</td>
<td>13,0</td>
<td>-95,6</td>
<td>-8,7</td>
</tr>
<tr>
<td>$1 \times 10^4$</td>
<td>0,0</td>
<td>0,1956</td>
<td>0,0</td>
<td>-97,5</td>
<td>-71,6</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>0,1956</td>
<td>0,4</td>
<td>-96,3</td>
<td>-55,7</td>
</tr>
<tr>
<td></td>
<td>$10^5$</td>
<td>0,098</td>
<td>11,8</td>
<td>-86,6</td>
<td>-15,8</td>
</tr>
</tbody>
</table>

**4. Conclusion**

The result of the study scientifically proves that the well support section experiences the main local sealing load in the interval of $0.4 \div 0.6 \times a$, that is, near the application of local pressure application. As an example, a section was considered at the point $x / a = 0.5$. At each section of the well support, the loads reach different values and do not depend on the adhesion of the cement stone to the casing and its strength properties. In the presence of strong compaction of the cement stone with the casing, the values of normal compressive stresses in the cement stone are much lower than in its absence, and the higher the mechanical strength of the cement stone, the higher the magnitude of the resulting compression stresses, which indicates a special distribution of the local load by the well support elements.
The study showed that the arising local stresses in absolute value in the casing are significantly higher than in the cement ring.

In the case of tight adhesion of the cement stone to the casing, the system perceives the load as a whole, and the value of the mechanical strength of the cement stone significantly affects the value of the created compressive stress. In the first case, they reach 100 MPa. In the second case, the picture is the opposite.

In the absence of adhesion of the casing to the cement, the maximum value of normal stresses along the cement ring can reach about 70 MPa. The resulting local sealing loads weaken the casing, which leads to accidents at the well.

The nature of lateral stress propagation is complex. First, in this case, there is no dependence of the mechanical strength of the stone. Secondly, it has a wavy character, which is explained by the different directions of their actions (clockwise or counterclockwise). As a result, the propagation of the arising local sealing stresses manifests itself on the deflection of the well support. In this case, the deflection is noted at a distance of about \( \pm 0.15 \times \) / a from the point of application of the crushing load.

Of particular importance is the presence of adhesion between the casing and the cement stone. The modern improvement of the well cementing technological process ensures a strong contact formed in the annulus.

Thus, as a result of theoretical studies and calculations, it can be assumed that the occurrence of complications caused by external local crushing loads is associated with the formation of normal stresses in the casing and cement stone. In absolute value, they can exceed the mechanical strength indicators of the elements of the "casing - cement stone" system.

References


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